CLASS : IX

Time : 3hrs. MM : 90

SECTION - A

Question numbers 1 to 8 carry 1mark each. For each question, four alternative choices have been provided of which only one is correct. You have to select the correct choice.

1. Which of the following is a rational number?

(A) $\frac{-2}{3}$ (B) $\frac{-1}{\sqrt{5}}$ (C) $\frac{13}{\sqrt{5}}$ (D) $\frac{\sqrt{2}}{3}$

2. The value of k, for which the polynomial x^3-3x^2+3x+k has 3 as its zero, is

(A) -3 (B) 9 (C) -9 (D) 12

3. Which of the following is a zero of the polynomial x^3+3x^2-3x-1?

(A) -1 (B) -2 (C) 1 (D) 2

4. The factorisation of $-x^2+5x-6$ yields:

(A) $(x-2)(x-3)$ (B) $(2+x)(3-x)$ (C) $-(x-2)(3-x)$ (D) $-(2-x)(3-x)$

5. In fig.1, $\angle DBC$ equals

(A) $40°$ (B) $60°$ (C) $80°$ (D) $100°$

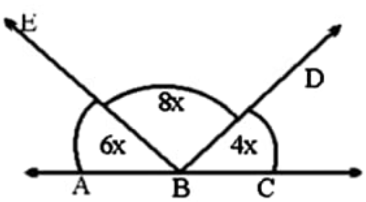


Fig.1

6. In fig.2, ABC is an equilateral triangle and BDC is an isosceles right triangle, right angled at D. $\angle ABD$ equals

(A) $45°$ (B) $60°$ (C) $105°$ (D) $120°$

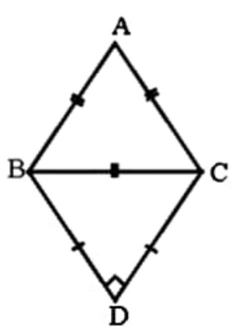


Fig.2

7. The sides of a triangle are 12cm, 16cm and 20cm. Its area is

(A) $48cm^2$ (B) $96cm^2$ (C) $120cm^2$ (D) $160cm^2$

8. The side of an isosceles right triangle of hypotenuse $4\sqrt{2}cm$ is

(A) 8cm (B) 6cm (C) 4cm (D) $4\sqrt{3}$cm

SECTION - B

Question numbers 9 to 14 carry 2 marks each :

9. If $x = 7+\sqrt{40}$, find the value of $\sqrt{x}+\frac{1}{\sqrt{x}}$

10. Factorise the polynomial: $8x^3 - (2x-y)^3$

11. Find the value of 'a' for which $(x-1)$ is a factor of the polynominal $a^2x^3-4ax+4a-1$

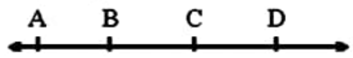
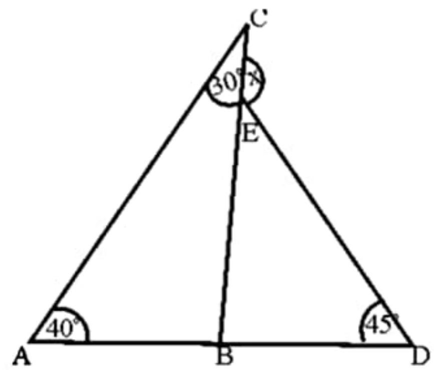


Fig. 3

12. In Fig.3, if AC=BD, show that AB=CD. State the Euclid's postulate/axiom used for the same.



13. In Fig.4 find the value of x.

Fig. 4

OR

In Fig.5, ABCDE is a regular pentagon. Find the relation between 'a' ,'b' and 'c'

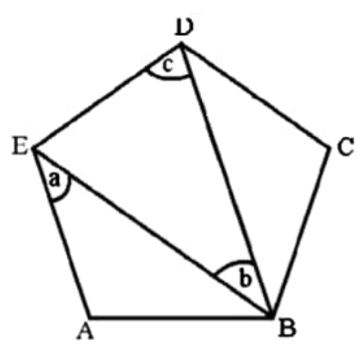


Fig. 5

14. In Fig.6, ABC is an equilateral triangle. The coordinates of vertices B and C are (3,0) and (–3,0)

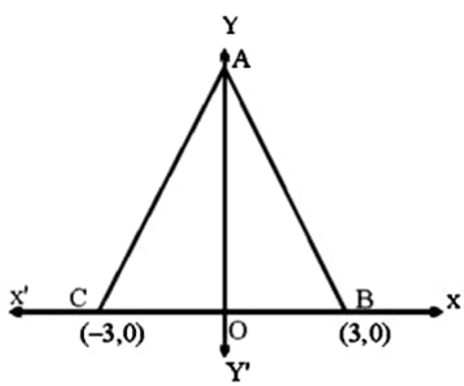


Fig. 6

respectively. Find the coordinates of its vertex A.

SECTION – C

Question numbers 15 to 24 carry 3 marks each:

15. **Evaluate :** $\left\{\sqrt{5+2\sqrt{6}}\right\}+\left\{\sqrt{8-2\sqrt{15}}\right\}$

OR

If $a=9-4\sqrt{5}$, Find the value of $a^2+\frac{1}{a^2}$

16. Simplify the following:

$$\frac{7+3\sqrt{5}}{3+\sqrt{5}}-\frac{7-3\sqrt{5}}{3-\sqrt{5}}$$

OR

If $\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}}=a+\sqrt{15}\,b$, find the values of a and b

17. Factorise the following:

$12(x^2+7x)^2-8(x^2+7x)(2x-1)-15(2x-1)^2$

18. Show that 2 and $-\frac{1}{3}$ are the zeroes of the polynomial $3x^3-2x^2-7x-2$.

Also, find the third zero of the polynomial

19. In Fig.7, $\ell \parallel m \parallel n$ and $a \perp \ell$. If $\angle BEF = 55°$, Find the values of x, y and z

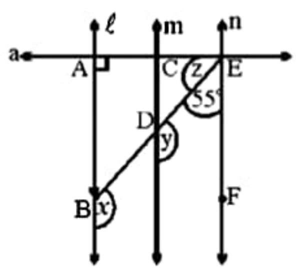


Fig.7

OR

In Fig.8, $\ell \parallel m \parallel n$. From the figure find the value of (y+x): (y-x)

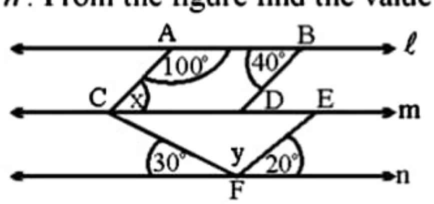


Fig.8

20. In Fig.9, DE||BC and MF||AB.

Find (i) $\angle ADE+\angle MEN$ (ii) $\angle BDE$ (iii) $\angle BLE$

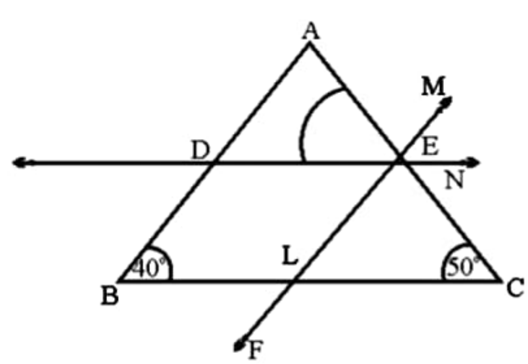


Fig.9

21. .... $\angle QPR$ and $PT \perp RQ$. Show that $\angle TPS = \frac{1}{2}(\angle R - \angle Q)$

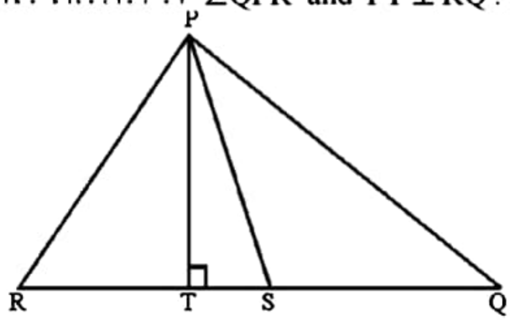


Fig.10

22. In Fig.11, ΔABC and ΔABD are such that AD=BC, $\angle 1 = \angle 2$ and $\angle 3 = \angle 4$. Prove that $BD = AC$

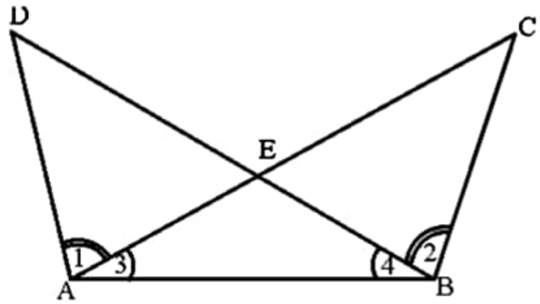


Fig.11

23. In Fig.12, AB||CD. If $\angle BAE = 50°$ and $\angle AEC = 20°$, find $\angle DCE$

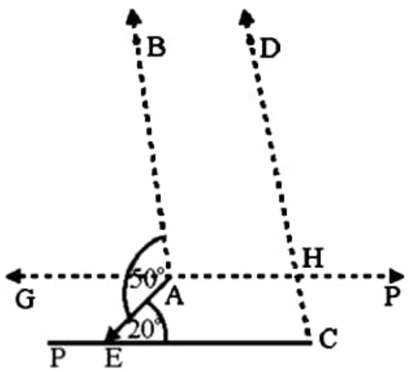


Fig.12

24. Find the area of a triangle whose perimeter is 180cm and two of its sides are 80cm and 18cm. Also calculate the altitude of the triangle corresponding to the shortest side.

SECTION-D

Question numbers 25 to 34 carry 4 marks each:

25. If $x = \frac{1}{2-\sqrt{3}}$, find the value of $x^3 - 2x^2 - 7x + 5$

OR

Simplify : $\frac{1}{1+\sqrt{2}} + \frac{1}{\sqrt{2}+\sqrt{3}} + \frac{1}{\sqrt{3}+\sqrt{4}} + \dots\dots\dots + \frac{1}{\sqrt{8}+\sqrt{9}}$

26. If $x=\dfrac{\sqrt{p+2q}+\sqrt{p-2q}}{\sqrt{p+2q}-\sqrt{p-2q}}$, then show that $qx^2-px+q=o$

OR

If $x=\dfrac{\sqrt{2}+1}{\sqrt{2}-1}$ and $y=\dfrac{\sqrt{2}-1}{\sqrt{2}+1}$, find the value of x^2+y^2+xy

27. If x^3+mx^2-x+6 has $(x-2)$ as a factor, and leaves a remainder n when divided by $(x-3)$, find the values of m and n.

28. Prove that $(x+y)^3+(y+z)^3+(z+x)^3-3(x+y)(y+z)(z+x)=2(x^3+y^3+z^3-3xyz)$

29. If A and B be the remainders when the polynomials $x^3+2x^2-5ax-7$ and $x^3+ax^2-12x+6$ are divided by $(x+1)$ and $(x-2)$ respectively and $2A+B=6$, find the value of 'a'

30. From Fig.13, find the coordinates of the points A,B,C,D,E and F. Which of the points are mirror images in (i) x-axis (ii) y-axis

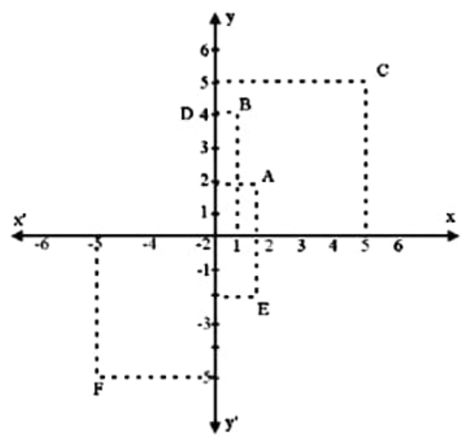


Fig.13

31. In Fig.14, $QT \perp PR$, $\angle TQR = 40^\circ$ and $\angle SPR = 30^\circ$. Find the values of x,y and z

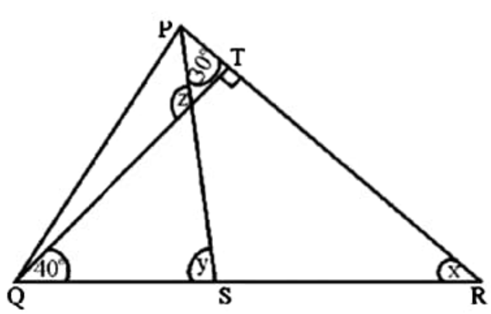


Fig.14

32. In Fig. 15, ABCD is a square and EF is parallel to diagonal BD and EM=FM Prove that

(i) DF=BE (ii) AM bisects $\angle BAD$

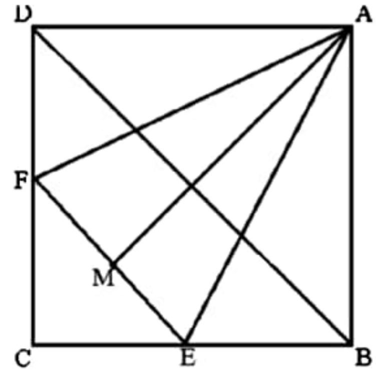


Fig.15

33. In Fig. 16, AB=BC, $\angle A = \angle C$ and $\angle ABD = \angle CBE$. Prove that CD=AE

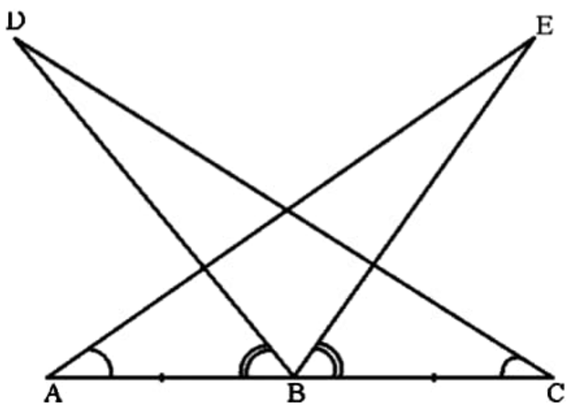


Fig.16

34. In Fig. 17, AB=AC, D is a point in the interior of ΔABC such that $\angle DBC = \angle DCB$. Prove that AD bisects $\angle BAC$ of ΔABC

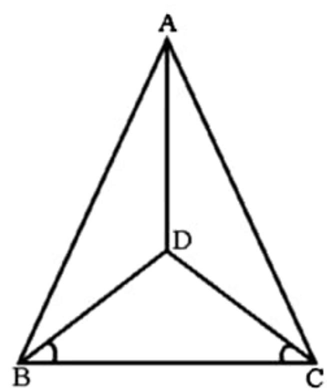


Fig.17